

Comparative modeling of the mitral valve in normal and prolapse conditions

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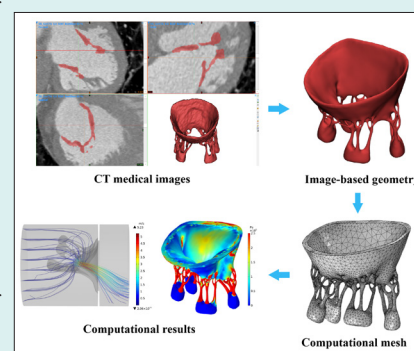
Abstract

Introduction: Computational modeling is one of the best non-invasive approaches to predicting the functional behavior of the mitral valve (MV) in health and disease. Mitral valve prolapse (MVP) due to partial or complete chordae tendineae rupture is the most common valvular disease and results in mitral regurgitation (MR).

Methods: In this study, Image-based fluid-structure interaction (FSI) models of the human MV are developed in the normal physiological and posterior leaflet prolapse conditions. Detailed geometry of the healthy human MV is derived from Computed Tomography imaging data. To provide prolapse condition, some chords attached to the posterior leaflet are removed from the healthy valve. Both normal and prolapsed valves are embedded separately in a straight tubular blood volume and simulated under physiological systolic pressure loads. The Arbitrary Lagrangian-Eulerian finite element method is used to accommodate the deforming intersection boundaries of the blood and MV.

Results: The stress values in the mitral components, and also flow patterns including the regurgitant flow rates are obtained and compared in both conditions through the simulation. These simulations have the potential to improve the treatment of patients with MVP, and also help surgeons to have more realistic insight into the dynamics of the MV in health and prolapse.

Conclusion: In the prolapse model, computational results show incomplete leaflet coaptation, higher MR severity, and also a significant increment of posterior leaflet stress compared to the normal valve. Moreover, it is found more deviation of the regurgitant jet towards the left atrium wall due to the posterior leaflet prolapse.



Introduction

Mitral valve prolapse (MVP) due to the chordae tendineae rupture is a significant cause of primary mitral regurgitation (MR). In many instances, MVP will not impact health, but when MR is severe, it can lead to serious complications, including stroke, atrial fibrillation, and heart failure.¹ Imaging techniques can visualize heart valves but do not provide valuable information about the causes of valve failure, structural dynamics, and hemodynamic parameters.^{2,3} Computational analysis is an example of a method that can be used to investigate the individual role of each component in the valve function, evaluate surgical repair, and also to improve the design of mechanical valves. Any destructive and pathological condition like MVP that alters the stress patterns inside

the valve components could affect the progression of valve disease.⁴ However, the assessment of stress within the MV apparatus is very challenging. Computational simulations also can fill this gap for researchers and surgeons by yielding accurate information about the deformation and stress patterns.^{5,6}

Simulation of the MV is a challenging biomechanical problem due to its highly complex structure and coupled interaction with the blood flow and pulsatile hemodynamic loads.^{3,7} However, recently due to advances in cardiac imaging and computational technology and the endeavors of many research groups, various computational simulations starting from simple 2D approximation to comprehensive 3D models have been developed.⁷ Finite Element (FE) analysis of the MV was first initiated by



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Kunzelman et al⁸ to examine leaflet deformations and stress patterns in the MV. That was the first 3D-FE model of the MV, including all essential anatomic components and regional tissue thickness. In a series of studies, Rim et al⁹⁻¹¹ developed a novel computational evaluation protocol to perform and compare two different virtual MV repair techniques in a patient with posterior mitral leaflet prolapse. Abedini and Johari Moghadam used Mooney-Rivlin hyperelastic model as material properties of leaflets' tissue for the first time among all models.¹² FE methods are suitable for the simulation of quasi-static events such as opened or closed valves. However, to accurately simulate transient dynamics and evaluate hemodynamics parameters, FSI models are required.³ Lau et al³ compared the effects of tubular and ventricular fluid domain geometries on the MV dynamic. It was shown that the predicted stresses were similar in both conditions, but the stresses and flow velocities values and also the valve closing configuration were slightly different. Later, Dahl et al¹³ developed an FSI algorithm for the simulation of the MV dynamics by rendering 2D asymmetric leaflets during left ventricular filling. Results indicated that important features of the flow field may not be predicted by the assumption of the symmetric model. Recently, Khodaei et al¹⁴ simulated the FSI model of MVP by considering the direct effect of left ventricular motion, and to take into account the prolapse effect as a result of chordal rupture, some chordae tendineae were removed from the model.

Computational results depend highly on the accuracy of valve geometry, material properties, and the transvalvular pressure load.⁶ In all the aforementioned studies, due to the complex structure of human MV components, the valve geometry usually was simulated with simplification assumptions. In the present study, the image-based and comprehensive geometry of the human MV with the realistic structure of chordae tendineae is derived from imaging data. Two normal and prolapsed valves are mounted in a rigid tube, and physiological systolic pressure is imposed at the inlet and outlet of this tube as boundary conditions. An FSI modeling approach based on ALE formulation is used in this study to allow for displacements of the boundaries due to the large deformation of the MV components. Important MV dynamic and hemodynamic parameters such as stress values in the leaflets and chords, velocity magnitudes and flow patterns in the fluid domain, and also backward flow rates into the left atrium are determined and compared in the normal and the prolapse conditions.

Materials and Methods

Geometry reconstruction from computed tomography (CT) images

It is a challenging problem to image and reconstructs high-quality geometry of the sub-valvular apparatus either with echocardiography or cardiac magnetic resonance imaging. CT imaging can advance the level of anatomical detail of

sub-valvular structures, especially the chordae tendineae.⁷ In this study, the geometries of models are based on CT image data of an adult male (67 years old) without any known history of the MV disease. A total of 337 axial, coronal, and sagittal image slices in the mid-diastolic phase are collected to reconstruct opened MV (Fig. 1). MIMICS commercial software is used for the segmentation and generation of the 3D MV model. This image-based model involves both leaflets, all recognizable chordae tendineae, and the upper parts of papillary muscles.

By convention, both the anterior (A) and the posterior (P) leaflets are divided into three individual segments: the anterior (A1 and P1), middle (A2 and P2), and posterior (A3 and P3) scallops.¹⁵ From the midline of the leaflets towards the commissure, the following chordae branches are inserted on each side of the leaflets: paramedial, main, commissural, and paracommissural chordae (only inserted on P1).¹⁵ Therefore, the reconstructed MV has thirteen chordae tendineae branches.

Prolapse in the posterior leaflet is more common than the anterior leaflet, mainly due to ruptured chordae in the central scallop (P2).¹⁶ Therefore, to consider the prolapse effect, the paramedial chords attached to this region are removed from the healthy model. Then, both normal and prolapse models are mounted separately in a straight tubular fluid volume so that their ventricular and atrial sections are chosen respectively intermediate volumes of 85 cm³ and 35 cm³.³

Material and governing equations

Fluid domain

Transmitral blood flow is modeled as a Newtonian viscous fluid. The continuity and momentum equations of incompressible, laminar fluid flow in ALE description are given as:

$$\nabla \cdot \mathbf{u}_f = 0 \quad (\text{Eq. 1})$$

$$\rho_f \frac{\partial \mathbf{u}_f}{\partial t} + \rho_f (\mathbf{u}_f - \mathbf{u}_m) \cdot \nabla \mathbf{u}_f = \nabla \cdot \boldsymbol{\tau} \quad (\text{Eq. 2})$$

Where ρ_f is the fluid density, $\mathbf{u}_f = [u \ v \ w]^T$ is the velocity vector, t is the time, $\boldsymbol{\tau}$ is the total stress tensor and \mathbf{u}_m is the velocity vector of the deforming mesh which is used in ALE formulation. The total stress tensor $\boldsymbol{\tau}$ for a generalized Newtonian fluid is defined by:

$$\boldsymbol{\tau} = -p\mathbf{I} + \mu \left[\nabla \mathbf{u}_f + (\nabla \mathbf{u}_f)^T \right] \quad (\text{Eq. 3})$$

Where p is the pressure, \mathbf{I} is the identity tensor, μ is the viscosity, and $[]^T$ shows the transpose of a matrix. The blood density and viscosity are assumed respectively $\rho_f = 1060 \left[\frac{\text{kg}}{\text{m}^3} \right]$ and $\mu = 0.004 \text{ [Pa.s)]}$.¹⁴

Solid domain

The equilibrium equations for solid mechanics are given by Newton's second law. Using the more common second

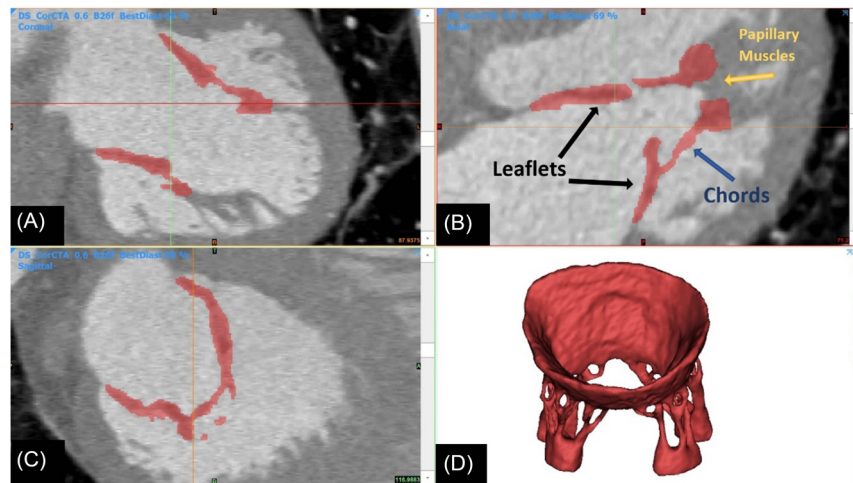


Fig. 1. Image-based construction of mitral valve geometrical model from (A) coronal, (B) axial, and (C) sagittal image slices. (D) generated 3D MV model in the mid-diastolic phase based on CT images.

Piola-Kirchhoff stress tensor, S , it is written as:

$$\rho_s \frac{\partial^2 d_s}{\partial t^2} = \nabla_x \cdot (FS)^T \quad (\text{Eq. 4})$$

where ρ_s is solid density, d_s is the vector of structural displacements, ∇_x is the gradient operator with respect to the material coordinates, and F is the deformation gradient tensor. The MV leaflets are assumed to be non-linear material due to their soft tissue reinforced by collagen fibers. A nearly incompressible isotropic Mooney-Rivlin hyperelastic material model is adopted.¹⁴ In this model, the strain energy density function (W) is a linear combination of the first I_1 and the second I_2 principal invariants of the right Cauchy-Green deformation tensor (C). Nine parameter Mooney-Rivlin material model defined as¹⁷:

$$W = C_{10}(\bar{I}_1 - 3) + C_{01}(\bar{I}_2 - 3) + C_{20}(\bar{I}_1 - 3)^2 + C_{02}(\bar{I}_2 - 3)^2 + C_{11}(\bar{I}_1 - 3)(\bar{I}_2 - 3) + C_{30}(\bar{I}_1 - 3)^3 + C_{03}(\bar{I}_2 - 3)^3 + C_{21}(\bar{I}_1 - 3)^2(\bar{I}_2 - 3) + C_{12}(\bar{I}_1 - 3)(\bar{I}_2 - 3)^2 + \frac{1}{2}\kappa(J - 1)^2 \quad (\text{Eq. 5})$$

$$J = \sqrt{\det(C)} = \det(F) \quad (\text{Eq. 6})$$

$$I_1 = \text{tr}(C), I_2 = \frac{1}{2} \left[(\text{tr}(C))^2 - \text{tr}(C^2) \right] \quad (\text{Eq. 7})$$

$$\bar{I}_n = J^{-\frac{2n}{3}} I_n, (n=1,2) \quad (\text{Eq. 8})$$

where C_{ij} , ($i + j \leq 3$) shows empirically determined material constants, \bar{I}_n shows a slightly different set of invariants, k is the bulk modulus, $\det(\cdot)$ is the determinant operator, $\text{tr}(\cdot)$ is the trace operator, and J is the determinant of the deformation gradient tensor and it shows also the ratio of the deformed elastic volume over the reference volume of materials. The strain energy density function is related to the second Piola-Kirchhoff stress tensor as:

$$S = 2 \frac{\partial W}{\partial C} \quad (\text{Eq. 9})$$

Empirical Material constants are obtained from mechanical test data reported by May-Newman and Yin.¹⁸ These constants and bulk modulus are determined in Table 1.

All the chordae tendineae are considered linear elastic material. By obtaining valid reference data, Young's modulus and Poisson's ratio of chordae tendineae are assumed respectively $E = 30$ MPa, $\nu = 0.45$.^{3,19} The density of the leaflets, as well as the density of chordae tendineae, are assumed to be $\rho_s = 1060 \left[\frac{\text{kg}}{\text{m}^3} \right]$.

Boundary conditions

This study focuses on MVP, in which only the MV closure stage is considered. A transmitral systolic pressure load based on clinical data is imposed at the inlet of the straight tubular fluid volume (Fig. 2).²⁰ Systolic pressure at the outlet of the tube is negligible and $P_{\text{outlet}}^f = 0$ is considered. In the solid domain, the mitral annulus upper surface and also papillary muscle volumes are considered to be fixed in the passage and do not participate in FSI.

Table 1. Mooney-Rivlin material coefficients for MV leaflets

Coefficient	Value (Pa)
C_{10}	25517.173
C_{01}	19445.891
C_{20}	13126.167
C_{02}	8157.79
C_{11}	10352.309
C_{30}	5488.58
C_{03}	2776.66
C_{21}	4376.38
C_{12}	3487.189
κ	44963064.684

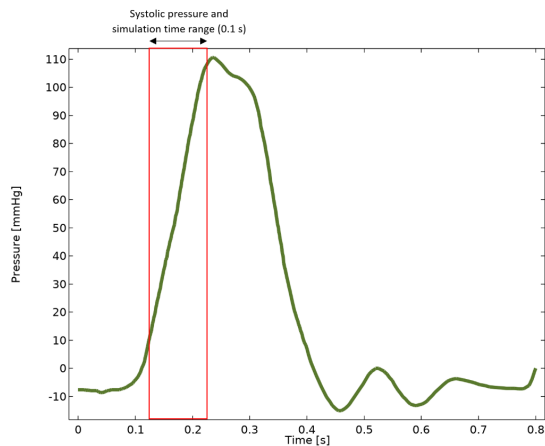


Fig. 2. Transmitral blood pressure load and imposed systolic pressure (0.12 to 0.22 seconds) at the inlet of the straight tubular fluid volume.²⁰

FSI coupling conditions include kinematic and dynamic constraints and have to be met at the interface boundary. The kinematic constraint (Eq. 10 and Eq. 11) fulfills the equality of displacement and velocity values in both domains at the interface. Whereas the dynamic constraint (Eq. 12) states that normal forces between the fluid and the solid at the interface boundary have to be equal. These constraints can be written as:

$$d_f = d_s, \quad (x, y, z) \in \Omega^{fs} \quad (\text{Eq. 10})$$

$$\frac{\partial d_f}{\partial t} = \frac{\partial d_s}{\partial t}, \quad (x, y, z) \in \Omega^{fs} \quad (\text{Eq. 11})$$

$$\tau_s \cdot \hat{n}_s = \tau_f \cdot \hat{n}_f \quad (\text{Eq. 12})$$

where d_f , d_s are respectively the vector of fluid and structural displacements, Ω^{fs} shows fluid-structure interface boundary, and \hat{n} is the unit vector normal to the interface of the fluid and solid boundary.

Numerical method

The solution of the incompressible Navier–Stokes equation in the flow solver is developed based on the ALE-FE formulation due to the large deformation of the mitral leaflets. In the ALE method, the fluid mesh deforms following the structural movement to avoid element distortion. The governing equations are discretized on unstructured triangular meshes and solved using COMSOL Multiphysics® version 5.4 commercial finite element package (Fig. 3). Due to restrictions in solving time and computer memory, the segregated solver approach is selected automatically by this software to solve involving equations.

The segregated solver approach subdivides the problem into two or more substeps so that each step represents a single physics and uses a damped version of Newton's method as the convergence criteria. In the fluid-structure interface, information for the solution is shared between the fluid solver and structure solver, and in this approach,

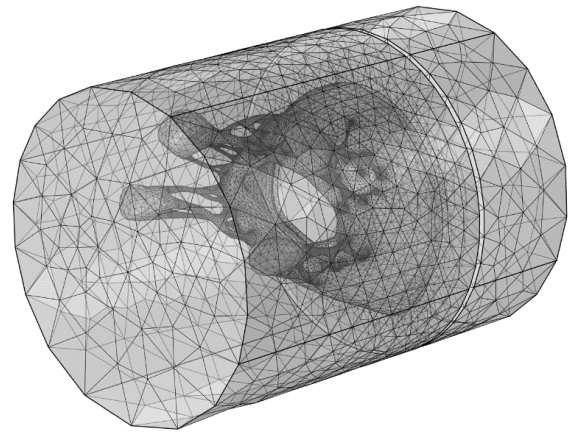


Fig. 3. Computational mesh discretization configuration.

the calculated forces acting on the structure are transferred to the structure side. Regardless of the approach to solving nonlinear problems, the solution is approached by iteration. That is, the used approach is called repeatedly, and gradually converges to the solution. With optimized iterative methods selected in COMSOL software, the error estimate in the solution was decreased with the number of iterations and, this convergence was quite monotonic.

Moreover, to control the numerical instabilities, Streamline-Upwind Petrov-Galerkin (SUPG) stabilization is used in the momentum equation. Time steps must be small enough for large deformations of the leaflets, so the optimal time step equal to 0.0002 (s) is chosen for the transient solution by applying the variable-order backward differentiation formula method with a maximum order of two. The grid independence study of the results has been carried out separately for both fluid and solid domains by several various mesh sizes. As a result, the fluid and solid domains are discretized respectively into 381914 and 101694 elements (a total of 483608) to accomplish the present study.

Results

Validation of the geometry accuracy

The reconstructed MV dimensions are compared with anatomical data in the literature to validate the model's accuracy (Fig. 4).^{21–23} As Table 2 shows, there is a good agreement between these data, so the accuracy of the extracted geometry is very reliable.

Stress values

The qualitative stress distributions across the atrial surfaces of leaflets with the configuration of MV closure in both normal physiological and prolapse conditions were shown in Fig. 5 at three representative times during the systolic phase. For better comparison, ventricular and three-dimensional views of stress distribution in the MV components were also demonstrated at peak systole ($t = 0.22$ s) in Fig. 6. The threshold of stress value (250 kPa) was applied to the simulation data to manifest alterations

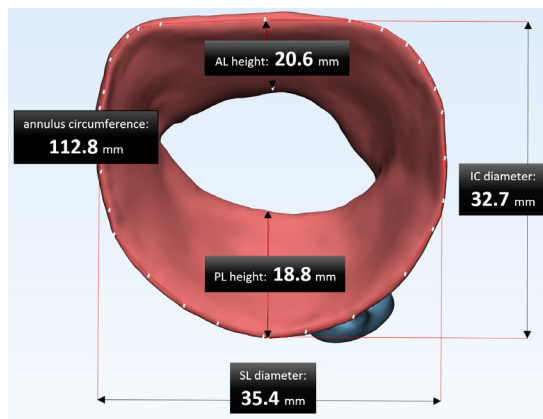


Fig. 4. The reconstructed MV dimensions; the measurements of intercommissural (IC) diameter, septo-lateral (SL) diameter, annulus circumference, anterior leaflet (AL), and posterior leaflet (PL) height.

of stress concentration accurately. Therefore, the stress values higher than this threshold were displayed in red.

As shown in Fig. 5 and Fig. 6, asymmetrical stress distribution patterns of the normal and the prolapsed MV were similar in the anterior leaflet but different in the posterior leaflet. A significant increase in regional stress following chordal rupture was found in the posterior leaflet. The high-stress concentration areas in the normal MV were found near the mitral annulus and the commissures. However, in the prolapse condition, the maximum stress concentrations occurred not only in the mentioned regions but also in the P2 and the P3 scallops. In both conditions, the posterior commissure underwent higher stress than the anterior commissure, and also the atrial surface of leaflets had a noticeable increase in stress compared to their ventricular surface at peak systole due to leaflets bending toward the left atrium (Fig. 6). Moreover, Fig. 5C and Fig. 6B (enclosed by the black circle) indicate incomplete leaflets coaptation and large deformation of posterior leaflet belly in prolapsed MV as a result of the chordal rupture.

In terms of stress values, there were high-stress concentrations (between 0.5 MPa and 2.5 MPa) close to the chordal insertion regions (Fig. 6A). However, across a large part of the leaflet surface, the range of stress values in

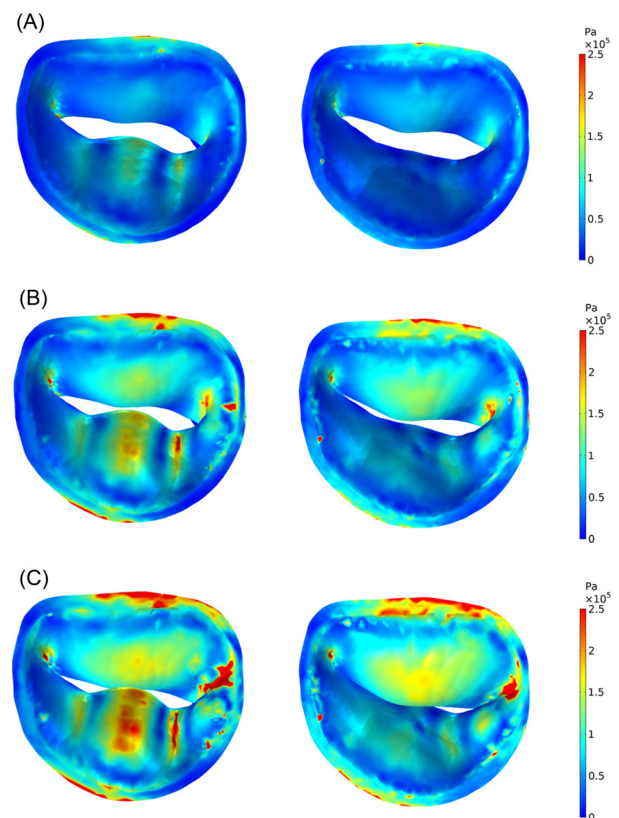


Fig. 5. Stress distributions (von Mises stress) across atrial surfaces of normal (right) and prolapsed (left) MV leaflets at: (A) $t = 0.1556$ s (start of the valve closure), (B) $t = 0.1994$ s, (C) $t = 0.22$ s (peak systole).

prolapsed MV (0–535 kPa) was higher than normal MV (0–180 kPa). The maximum stress value of the anterior and the posterior leaflet occurred respectively in A2 and P3 scallops. The average stress values during systole in the MV scallops were demonstrated in Fig. 7. It was shown in Fig. 7 that the average stress value in each anterior scallop of normal MV did not change significantly compared to the prolapse condition, and the most change was related to the A1 zone, in which it was decreased by 6.74%. However, mean stress variations were most apparent in the posterior leaflet, and it increased sharply by 81% in the P3 scallop (See Table 3).

Computational results showed higher stress magnitudes

Table 2. Main dimensions of image-based geometry compared with data in the literature

Main parameters of mitral geometry	Data in the literature (mm) ^{21–23}		Image-based MV dimensions (mm)
	Range	Mean \pm SD	
Intercommissural (IC) diameter	27–51	39.3 \pm 4.6	35.4
Septo-lateral (SL) diameter	19.5–42.5	31.4 \pm 4.5	32.7
Anterior leaflet (AL) height	11.1–37.4	25 \pm 7	20.6
Posterior leaflet (PL) height	10.8–34	22 \pm 6.6	18.8
Mitral annulus circumference	85–148	119.8 \pm 12.6	112.8
Anterior chordae tendineae height	9.5–23.5	14.5	14.7
Posterior chordae tendineae height	8–19	13	14.2

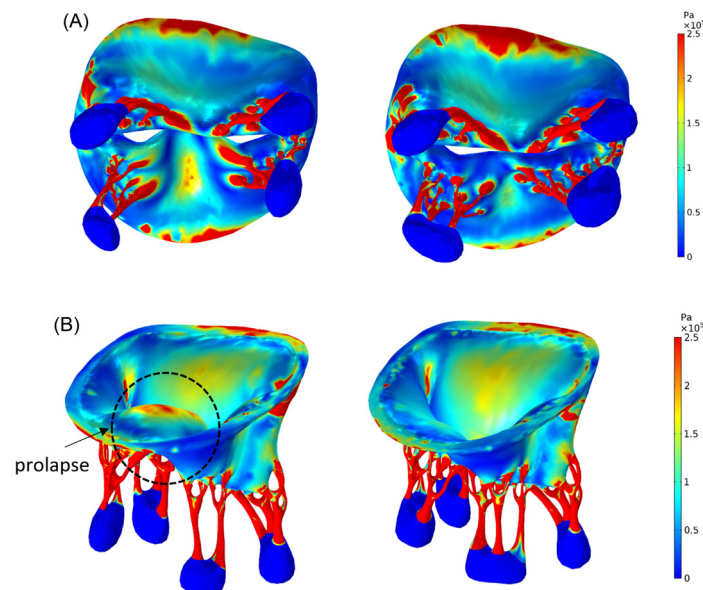


Fig. 6. Stress distributions (von Mises stress) in the normal (right) and prolapsed (left) MV at peak systole; (A) ventricular view (B) three-dimensional view. The prolapse of the posterior leaflet is obvious in (B).

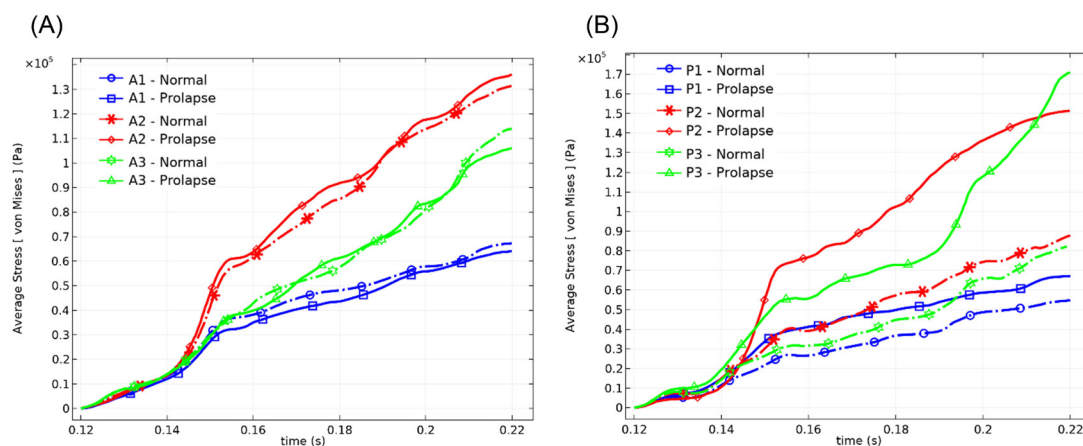


Fig. 7. Average stress values in the (A) anterior scallops, and (B) posterior scallops during systole.

(0–19 MPa) in the chordae tendineae with respect to the leaflets. The mean stress values during systole in all chordae tendineae branches also were illustrated in Fig. 8. It can be seen from Fig. 8 that the mean stress in the chords attached to the anterior leaflet was higher than posterior chords in the case of the normal valve. The stress values in chordae tendineae decreased by moving away from the midline of the leaflets towards the commissures.

Posterior leaflet Prolapse did not have much effect on the mean stress of the anterior chords, and most changes were seen at the commissural chords of the anterior leaflet due to the connection of these chords to both leaflets. As expected, in the absence of the posterior paramedial chords, the adjacent main chords are forced to withstand a lot of tension. Therefore, most of the changes in the mean and maximum stress occur in these chords. More detailed information about stress values of the MV components

and their differences rate caused by chordal rupture are reported in Table 3.

Transmitral flow field and mitral regurgitation

The streamlines of transmitral blood flow, as well as the blood velocity magnitudes, are presented in Fig. 9 at peak systole to compare the flow field between the normal and the prolapsed models. From Fig. 9 it is evident that the maximum velocity occurred in the leaflets in the adjacency of the coaptation region. In the prolapse condition, it can be seen more deviation of the regurgitant jet toward the left atrium wall due to the posterior leaflet bulging. Moreover, the cross-sectional area of the regurgitant jet is significantly larger in the prolapsed MV.

In terms of blood velocity magnitudes, the maximum speed value in the prolapse condition ($5.23 \frac{m}{s}$) does not change much compared to the normal MV ($5.31 \frac{m}{s}$) and

Table 3. mean and maximum stress values in the MV components and differences rate caused by chordal rupture

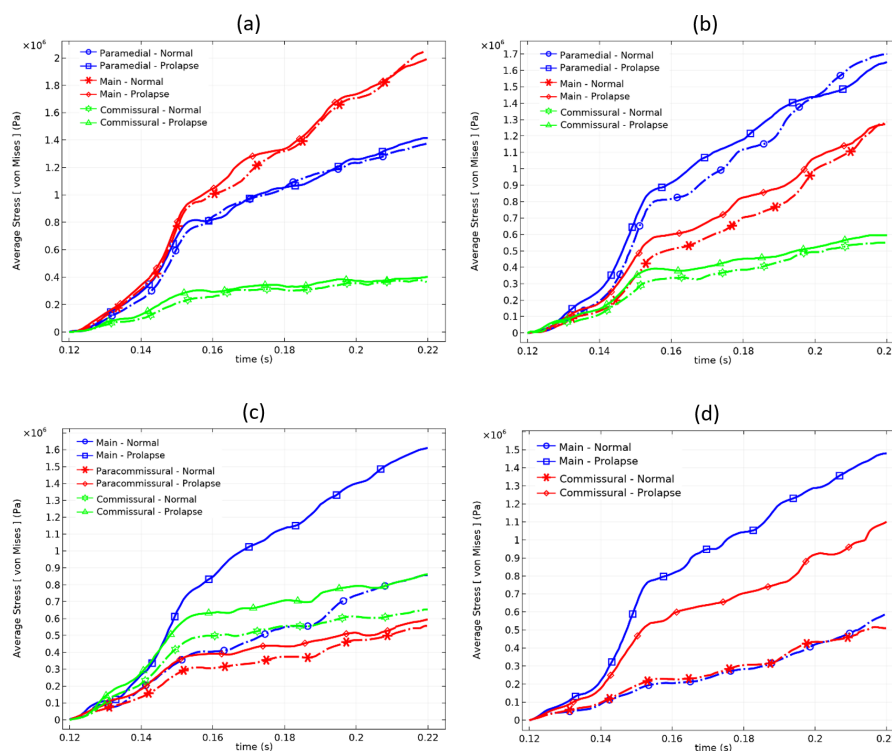
Region		Mean stress ^a (kPa)		Difference ^b (%)	Maximum stress (kPa)		Difference (%)
		Normal	Prolapse		Normal	Prolapse	
Anterior leaflet scallops	A1	38.60	36.00	- 6.74	122.00	125.30	+ 2.70
	A2	68.60	71.70	+ 4.51	180.00	200.00	+ 11.11
	A3	51.00	50.60	- 0.78	172.20	146.00	- 15.21
Posterior leaflet scallops	P1	30.00	40.00	+ 33.33	91.20	169.60	+ 85.96
	P2	45.60	81.50	+ 78.72	127.60	248.70	+ 94.90
	P3	38.40	69.50	+ 80.99	145.20	534.50	+ 268.11
The chordae tendineae attached to A1	Paramedial	815	836	+ 2.57	7578	7211	- 4.084
	Main	1065	1100	+ 3.29	19205	18700	- 2.63
	Commissural	247	273	+ 10.52	1538	1346	- 12.48
The chordae tendineae attached to A3	Paramedial	885	937	+ 5.86	12950	8043	- 37.89
	Main	568	649	+ 14.26	6079	4887	- 19.60
	Commissural	324	368	+ 13.58	3369	3603	+ 6.95
The chordae tendineae attached to P1	Paramedial	501	Ruptured	-	7784	Ruptured	-
	Main	458	900	+ 96.5	4754	15787	+ 232.70
	Paracommissural	313	368	+ 17.57	2566	2041	- 20.46
The chordae tendineae attached to P3	Commissural	443	571	+ 28.89	3408	3983	+ 16.87
	Paramedial	550	Ruptured	-	14610	Ruptured	-
	Main	256	836	+ 226.56	2458	18953	+ 671.07
	Commissural	263	581	+ 120.91	4624	12341	+ 166.89

^a von Mises stresses.^b Compared to normal physiological condition; + increase, - decrease.

is decreased very slightly (by 2%). Numerical results show that the average blood velocity magnitude in the coaptation region of prolapsed valve ($2.76 \frac{m}{s}$) is also approximately 6% less than the normal MV ($2.94 \frac{m}{s}$).

Fig. 10 indicates the instantaneous regurgitant volume

during the whole systole for both conditions. The highest blood volume passing through the normal and prolapsed MV occurred respectively at $t = 0.147$ s and $t = 0.156$ s. After this time, the transmitral flow rate started declining slightly in the prolapse case, whereas it took place on a steeper slope in the normal valve. The total regurgitant

**Fig. 8.** Average stress values in the chordae tendineae attached to (A) A1, (B) A3, (C) P1, and (D) P3 scallops during systole.

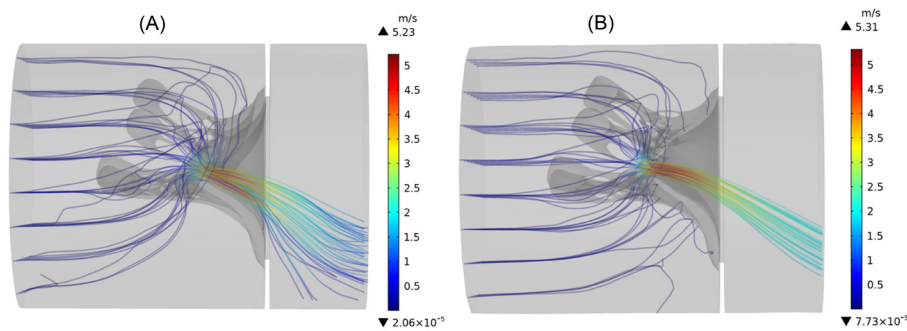


Fig. 9. The instantaneous streamlines of transmitral flow, colored by the velocity magnitude at peak systole. (A) prolapsed MV (B) normal MV.

volume in the normal valve is calculated 21.03 mL, and by a 63% increase, it is 34.22 mL in the prolapsed valve.

Discussion

The posterior leaflet dysfunction due to its acute chord rupture is a common MV disease, and clinical techniques cannot yield any valuable information about pathological MV dynamics. Therefore, this paper presents two computational FSI models of the realistic human MV within the ALE framework to find out the effects of the posterior chordal rupture in the MV function. An accurate and reliable MV geometry reconstruction is the principal step in the MV simulations.⁷ The previous studies usually modeled the MV under geometrical simplification. For example, as the earliest studies, Kunzelman et al²⁴ and Lau et al³ simulated MV dynamics with symmetric and uniform-thickness geometries. More recently, Khodaei et al¹⁴ and Caballero et al²⁵ also investigated the impact of chordae rupture on the left heart dynamics with cable-like structures of chordae tendineae. Although these studies have significantly improved cardiac simulations, sometimes simplifying the simulation geometry can misrepresent the results in pathological states. To the best of the authors' knowledge, this is the first time that an individualized and comprehensive MV geometry is derived from CT imaging data by considering all details

of the geometry, especially the intricate and non-uniform structures of the chordae tendineae, and then it is got involved in the computational FSI simulation.

In the present study, the maximum and average amount of stress exerted on the leaflets and chordae tissues is determined during the systolic phase. In the normal physiological condition, it is shown that the average stress value across the anterior leaflet is greater than the posterior leaflet, and the maximum stress value is located on the anterior leaflet belly. These features were observed in almost all the previous studies.⁷ The mitral leaflets' stress values reported by earlier computational studies seem higher than our predictions.²⁶⁻²⁹ The main discrepancy between the stress values in this paper and the other computational studies could arise from the individualized features of the current simulation geometry, such as the difference in the non-uniform thickness of the leaflets, and the presence of the complex and realistic structures of the chordae tendineae. From Fig. 7A, Fig. 8A, and Fig. 8B, it is clear that stress increment in the MV components is with a steep slope before the start of valve closure ($t \cong 0.15$ s), and after that, it increases with a gentle slope. It is worth noting that this issue occurs in the prolapse condition as well. Similar to Caballero et al²⁵ investigations, the numerical results of the healthy valve also show that the chordae tendineae branches attached to the central region (P2 and A2) of the leaflets are recognized as the load-bearing chords, and carry the majority of the systolic load exerted on the MV apparatus.

The comparison of numerical results shows that the pathological state of chordal rupture severely affected the MV function. The chordae tendineae rupture leads to a significant change in the configuration of MV closure and the development of a large bulging area in the middle scallop of the posterior leaflet known as the prolapse. Similar to the previous findings,^{24,25} the chordal rupture causes the stress increment in MV components, notably in the P2 and P3 scallops and the adjacent remaining main chordae as reported in Table 3. It is noteworthy that the posterior leaflet prolapse also alters the stress distribution in the anterior leaflet. However, it does not involve any considerable changes in the stress levels of this leaflet.

In terms of transmitral flow, the determined velocity

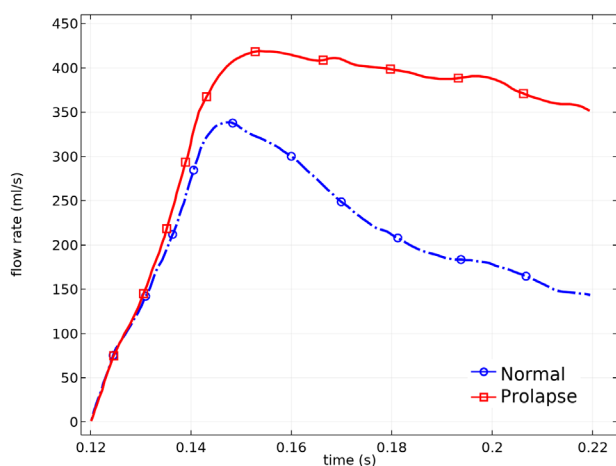


Fig. 10. Flow rate across the MV during the whole systole.

Research Highlights

What is the current knowledge?

✓ Mitral valve simulation with simplifications of geometry such as symmetric leaflets with a uniform thickness or manual designing, etc.

What is new here?

✓ An individualized and comprehensive mitral valve geometry is derived from Computed Tomography imaging data.

✓ Considering key elements of the geometry, especially the intricate and non-uniform structures of the chordae tendineae.

✓ Analysis of the mitral valve mechanical behaviors simultaneously in healthy and prolapse conditions

magnitudes demonstrate a reasonable agreement with the previous computational and echocardiography velocity measurement studies.^{25,30–32} As can be seen in Fig. 9B, the posterior leaflet prolapse forces the regurgitant jet to deviate towards the atrium wall. The numerical results also show that incomplete leaflets coaptation and consequently a larger closure orifice in prolapsed MV leads to the decrement of the average velocity in the vicinity of the coaptation region. Furthermore, according to the calculated total regurgitant volume during the systole and the classification of Lancellotti et al,³³ the severity of MR in the normal and prolapse models are placed respectively in ‘mild’ and ‘moderate’ ranges.

This study presented the qualitative and quantitative description of the mitral valve behavior simultaneously in the normal physiological and prolapse conditions to distinguish better the differences between both states. Despite some simulation simplifications, computational results showed a reasonable agreement with the data available in the valid references. Simulations of a mitral valve coupled with the detailed and image-based left ventricle and aortic valve geometries under realistic boundary conditions, such as movements of the left ventricle and papillary muscles could be the next advancement in this field. These simulations also highlight the importance of computational modeling in yielding reliable information data that are not obtainable by clinical measurements.

Conclusion

In this study, a detailed MV geometry was derived from CT images with acceptable accuracy for the first time and then it was embedded in the computational FSI simulations. It was found that the manipulated Galerkin finite element method coupled with realistic material properties and boundary conditions could predict the MV behavior robustly. This model also had a significant improvement compared to the previous studies because it provides the mitral valve functional parameters in the

form of quantitative and comparative data simultaneously in both normal and pathological conditions. In the normal physiological condition, it was shown that the middle scallops of the leaflets and their related chords carry the majority of the systolic load, and these regions are disposed to rupture. The posterior leaflet prolapse due to chordal rupture led to significant stress changes in the MV components, greater regurgitant flow rate, and also more deviation of the regurgitant jet to the atrium wall. These abnormalities may reduce the MV life and lead to chronic diseases in the future. Therefore, detailed information released in this study offers comprehensive insight to the surgeons for improving the surgical outcome and the procedures of the MV repair in the posterior leaflet prolapse condition.

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Authors' contribution

SER: conceptualization, supervision, study consultation, and project administration.

AT: Geometry reconstruction, simulation design, study validation, data presentation, data analysis, data presentation, writing and reviewing.

Ethical Issues

There is none to be declared.

Competing interests

The authors declare no competing interests.

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